# EMT 101- Engineering Programming Homework 3 

Handed out 25/11/2014

## 1 Contour and Surface Plots(30 \%)

You are to create a three-dimensional plot of the function

$$
\begin{equation*}
z=f(x, y)=\left(x^{2}+y^{2}\right) \frac{\sin (y)}{y} \tag{1}
\end{equation*}
$$

over domain $-10 \leq x \leq 10$ and $-10 \leq y \leq 10$.

Can you detect there is a problem with the function? If yes, please rectify the problem.

Once rectified, please use the available MATLAB function meshgrid to create a mesh based on $f(x, y)$. Type help meshgrid to understand more on using the function.

Plot the following:

1. The mesh of the system $z=f(x, y)$
2. The 2 D contour map of the system
3. The 3D surface plot with 2D contour map drawn beneath.

## 2 Free Vibration Response of Undamped Single Degree of Freedom System(70 \%)

The free vibration response of an undamped single degree of freedom (SDOF) oscillator is given by its displacement $x(t)$ satisfying

$$
\begin{equation*}
x(t)=x(0) \cos (\omega t)+\frac{v(0)}{\omega} \sin (\omega t) \tag{2}
\end{equation*}
$$

where $t$ is time in seconds and $\omega=\sqrt{\frac{k}{m}}$ is the natural frequency of the system with $m$ and $k$ being the mass and the stiffness of the system. Define $v(t)$ as the time dependent velocity of the system. Determine $v(t)$.

Write an M-file using functions that will compute and plot

1. The displacement of the system $x(t)$ as a function of time
2. The velocity of the system $v(t)$ as a function of time
for time interval $0 \leq t \leq 10 \mathrm{~s}$. Assume $m=10, k=1$ and that $x(0)=v(0)=10$.

Note that both $x(t), y(t)$ should be on ONE plot. Use the a solid line for the displacement and broken-lines for the velocity.

To ensure that your plot will be reasonably smooth, choose an increment in your displacement and velocity calculations that is no larger than $1 / 10$ th of the system period $T=2 \Pi \sqrt{m / k}$.

Using the period estimation, can you verify if your computations are correct?


Fig. 1: Vibration of the System.

